

4-28

[ WE CHECKED EX. 22 TODAY ]

OTHER EXAMPLES OF USING THE BASIC TRUTH TABLES  
TO FIND MORE COMPLICATED TRUTH TABLES

•  $(\sim a) \cup (\sim b)$

a	b	$\sim a$	$\sim b$	$(\sim a) \cup (\sim b)$
T	T	F	F	F
T	F	F	T	T
F	T	T	F	T
F	F	T	T	T

•  $\sim(a \cup b)$

a	b	$a \cup b$	$\sim(a \cup b)$
T	T	T	F
T	F	T	F
F	T	T	F
F	F	F	T

•  $a \rightarrow \sim b$

a	b	$\sim b$	$a \rightarrow \sim b$
T	T	F	F
T	F	T	T
F	T	F	T
F	F	T	T

### 3 VARIABLE EXAMPLE

a, b, c

a	b	c	COMPOUND STATEMENT
T	T	T	
T	T	F	
T	F	T	
T	F	F	
F	T	T	
F	T	F	
F	F	T	
F	F	F	

### VALIDITY OF AN ARGUMENT

WE USE TRUTH TABLES FOR EACH STATEMENT IN AN ARGUMENT TO CHECK VALIDITY

- FORM A TRUTH TABLE FOR EACH STATEMENT
- LOOK AT ROWS THAT HAVE TRUE PREMISES. (ONLY THESE ROWS MATTER)
- IF ANY OF THESE ROWS HAS A FALSE CONCLUSION, THE ARGUMENT IS INVALID. OTHERWISE, THE ARGUMENT IS VALID.

FOR AN ARGUMENT OF THE FORM  $P_1, P_2, C$ ,

a	b	c	P1	P2	C
⋮			⋮	⋮	⋮
			T	T	T
⋮			⋮	⋮	⋮
			T	T	F
⋮			⋮	⋮	⋮

← LOOK FOR 'TTF'

APPLY TO THE DOG - ANIMAL - EATING THING ARGUMENT.

P<sub>1</sub> IF DOG, THEN ANIMAL.

d = DOG

P<sub>2</sub> IF ANIMAL, THEN EATING THING.

a = ANIMAL

C IF DOG, THEN EATING THING.

e = EATING THING

P<sub>1</sub> d → a

P<sub>2</sub> a → e

C d → e

d	a	e	P <sub>1</sub> d → a	P <sub>2</sub> a → e	C d → e
T	T	T	T	T	T
T	T	F	T	F	F
T	F	T	F	T	T
T	F	F	F	T	F
F	T	T	T	T	T
F	T	F	T	F	T
F	F	T	T	T	T
F	F	F	T	T	T

NO 'TTF'  
SO VALID