

16-2015

ENERGY AND WORK

WORK - AN CHANGE IN ENERGY FROM ONE FORM TO ANOTHER

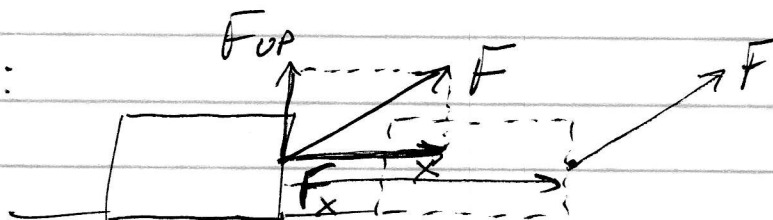
- A FORCE EXERTED THROUGH A DISTANCE
- A SCALAR VALUE

$$W = (\text{FORCE IN DIRECTION OF } x) \times (\text{DISTANCE } x)$$
$$W = F \cdot x$$

$$\text{UNITS: } N \cdot m \text{ or } \frac{kg \cdot m^2}{s^2}$$

$$1 J = 1 \text{ JOULE} = 1 \frac{kg \cdot m^2}{s^2} = 1 N \cdot m$$

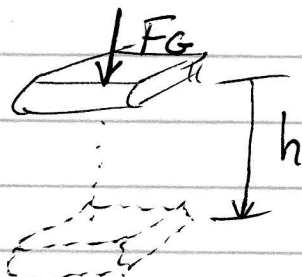
EXAMPLE:



WORK DONE BY $F_{up} = 0$

$$WORK = F_x \cdot x$$

EXAMPLE:

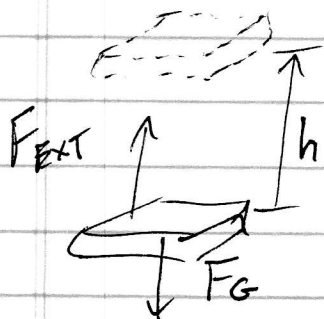


"BY A FORCE"

$$W_G = F_g \cdot h = mgh$$

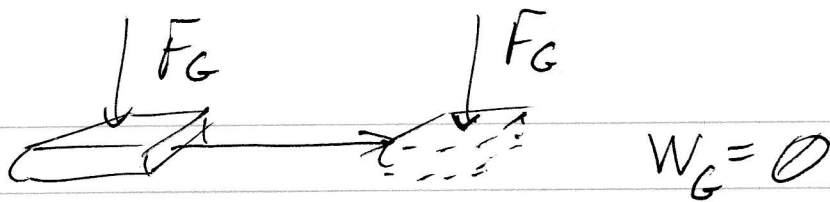
F_g IS IN DIRECTION OF MOTION, SO

$$W_G > 0$$



$$W_G = -F_g \cdot h$$
$$= -mgh$$

"AGAINST A FORCE"



WORK DOESN'T DEPEND ON THE OBSERVER'S
FRAME OF REFERENCE { POSITION
VELOCITY

ENERGY

THE ABILITY TO DO WORK BASED
ON AN OBJECT'S POSITION AND OR
VELOCITY.

UNITS: JOULES S.I.
(U.S. POUND-FOOT)

OTHER UNITS: erg
KWHOURS
AMP HOURS
CALORIES
B.T.U.
⋮

TYPES OF ENERGY: MECHANICAL • POTENTIAL { POSITION
↑ • KINETIC { MOTION

COMPUTE FROM
 $h, v, r, \text{etc.}$

DISSIPATIVE • HEAT, THERMAL
(HARDER TO MEASURE) FLUID MOTION

FORMS OF ENERGY

GRAVITATIONAL (MECHANICAL) (POTENTIAL)

SPRING OR ELASTIC (MECHANICAL) (POTENTIAL)

KINETIC (MECHANICAL) (KINETIC)

LIGHT OR ELECTRO-MAGNETIC RADIATION

NUCLEAR

FOOD CALORIES

THERMAL

WIND / WATER / FLUID

ELECTRO-MAGNETIC

CHEMICAL

SOUND WAVES

⋮

KINETIC ENERGY (ENERGY OF MOTION)

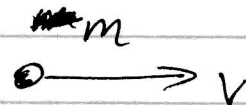
$$K = \frac{1}{2} m v^2$$

$$\left(\text{kg} \left(\frac{\text{m}}{\text{s}}\right)^2 = (\text{J})\right)$$

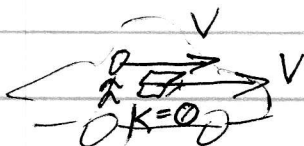
• SCALAR

• ALWAYS NON-NEGATIVE

• DIRECTION IS UNIMPORTANT



VALUE DEPENDS ON OBSERVER

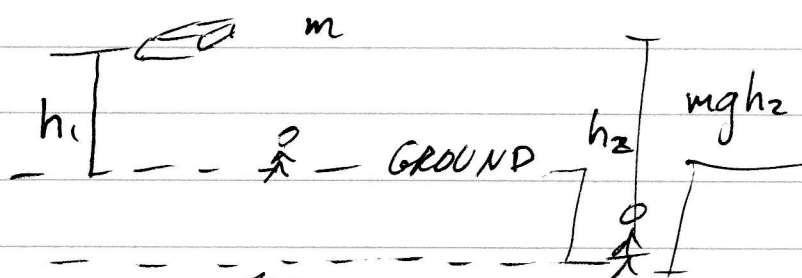


$$K = \frac{1}{2} m v^2$$

GRAVITATIONAL POTENTIAL ENERGY

$$P_G = mgh$$

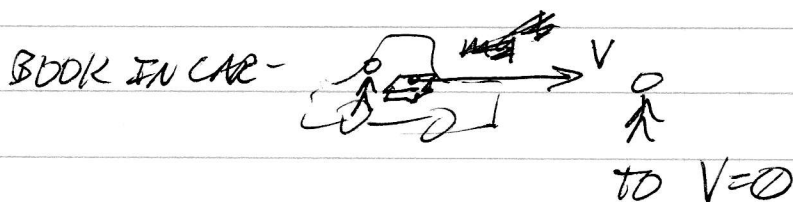
$(\text{kg} \cdot \frac{\text{m}}{\text{s}^2} \cdot \text{m})$
 (J)



DEPENDS ON THE OBSERVER

P_G IS NOT INTRINSIC TO BOOK,
IT IS DUE BOOK-EARTH SYSTEM

WORK = CHANGE IN ENERGY IS SAME
FOR ALL OBSERVERS



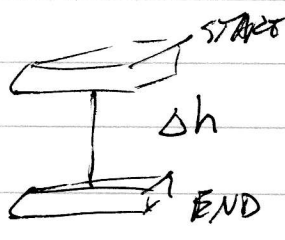
$$\Delta K = \text{CHANGE IN KINETIC ENERGY}$$

$$= 0 - \frac{1}{2}mv^2$$

BOTH AGREE ON V CHANGE
SO BOTH AGREE ON ΔK

$$\text{WORK} = \Delta K$$

BOOK IN GRAVITY FIELD



$$P_{\text{TOP}} = mgh_{\text{TOP}}$$

$$P_{\text{BOTTOM}} = mgh_{\text{BOTTOM}}$$

$$\Delta P = mg\Delta h$$

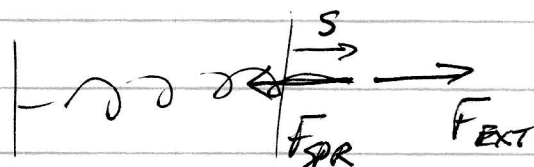
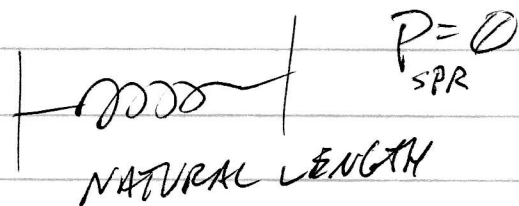
$$= \text{WORK}$$

ELASTIC ENERGY

$$W_{\text{SPR}} = -F_{\text{SPR}} \cdot s$$

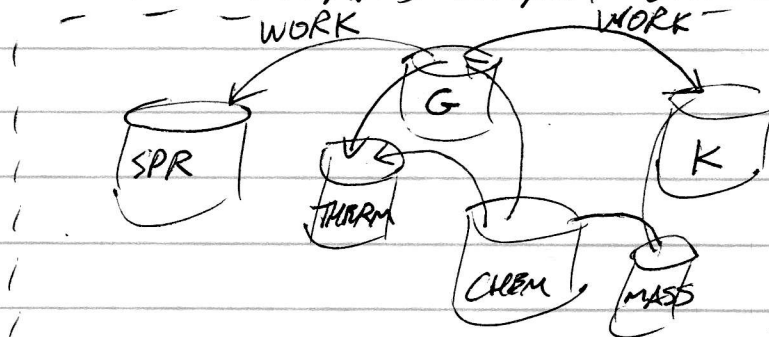
$$P_{\text{SPR}} = \frac{1}{2} k s^2$$

$$\left(\frac{\text{N}}{\text{m}}\right)(\text{m})^2 = (\text{N} \cdot \text{m}) = (\text{J})$$



P_{SPR} IS 0 OR POSITIVE

HOW DO ~~WORK~~ WORK AND ENERGY CAUSE MOTION?



ISOLATED SYSTEM

TOTAL ENERGY = CONSTANT

$$E = mc^2$$

IN AN ISOLATED SYSTEM, TOTAL ENERGY IS CONSTANT.

CONSERVATION OF ENERGY

SOME TIMES MECHANICAL ENERGY IS CONSERVED

(ONLY HAVE CONSERVATIVE FORCES: GRAVITY, ELASTIC, ELECTRIC)

(NO DISSIPATIVE FORCES: FRICTION, DRAG)

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PRINCIPLE OF WORK AND ENERGY (KINETIC)

$$W_{\text{NET}} = \Delta K$$

MOTION

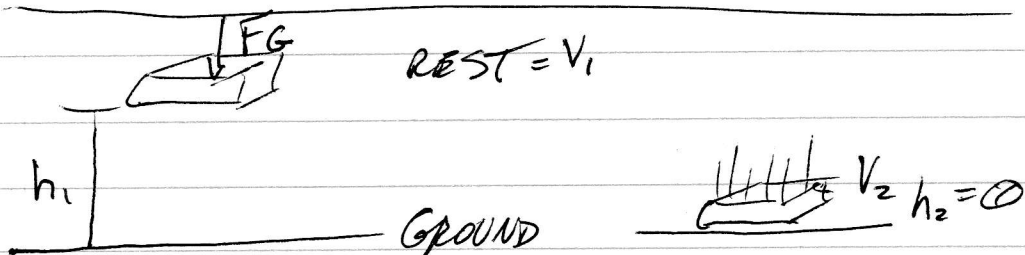
$$\text{OR } K_2 - K_1 = W_{\text{NET}}$$

OR

$$K_2 = K_1 + W_{\text{NET}}$$

FORCES ACTING
THRU DISTANCE

APPLY THE LAW OF CONSERVATION OF ENERGY



HOW FAST IS IT MOVING BEFORE IT HITS?

START

$$P_{G_1} + K_1 \overset{?}{=} P_{G_2} + K_2$$

(IGNORE AIR RESISTANCE)

$$mgh_1 = \frac{1}{2}mv_2^2$$

$$v_2 = \sqrt{2gh_2}$$

DOESN'T DEPEND
ON MASS

(SAME ANSWER AS USING NEWTON'S LAW)